

x & y intercepts

$f(x) = y$ is a function

x-intercept : Substitute $y=0$ and solve for x

(At these values of x , the graph crosses the x -axis.)

y-intercept : Put $x=0$, compute y , this is the y -intercept

(At these values of y , the graph intersects the y -axis.)

Ex) $f(x) = y = x^2 + x - 2$

x-intercept : $x^2 + x - 2 = 0 \Rightarrow (x+2)(x-1) = 0 \Rightarrow x = -2, x = 1$

Therefore the graph intersects the x -axis at these points.

y-intercept : Put $x=0$, get $y = -2$

The graph intersects the y -axis at this point

Ex) $f(x) = x^3 - 33x^2 + 216x - 2$

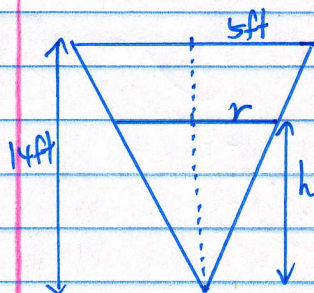
x-intercept : $x^3 - 33x^2 + 216x - 2 = 0$, solutions of this equation.

y-intercept : -2

Ex) A tank of water in the shape of a cone is leaking water at a constant rate of $2 \text{ ft}^3/\text{hr}$. The basic radius of the tank is 5 ft and the height is 14 ft

a) At what rate is the depth of water changing when the depth is 6 ft ? $\frac{dh}{dt}$

b) At what rate is the radius of the top of the water changing when the depth is 6 ft ? $\frac{dr}{dt}$



Given: $\frac{dv}{dt} = -2$

$V = \frac{1}{3} \pi r^2 h$

Asking for $\frac{dh}{dt}$; $\frac{dr}{dt}$

$\frac{dv}{dt} = \frac{1}{3} \pi r^2 \frac{dh}{dt} + \frac{1}{3} \pi r^2 \frac{dh}{dt}$

$= \frac{2}{3} \pi \left(\frac{5h^2}{14} \right) \frac{dr}{dt} + \frac{1}{3} \pi \left(\frac{25h^2}{14 \times 14} \right) \frac{dh}{dt}$

Substitute this in the formula for V

$V = \frac{1}{3} \pi \left(\frac{5h^2}{14} \right) x h$